# Applying the direct duplicate method to simulated IDCR/SOWER survey data

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## ABSTRACT

The direct duplicate method (Palka, 1994) was applied to simulated IDCR/SOWER survey data. Estimates of whale density were generally negative biased, but less so than estimates obtained using the standard method. The mean bias across scenarios was -11% (range -31% to 8%) for the "2004" scenarios and -5% (range -19% to 10%) for the "2005" scenarios. Negative bias was more pronounced when a density gradient was present, when the detection function used to generate the simulated sightings excluded school size but included weather as a covariate, when errors in recorded school size were introduced, when weather and density were correlated, and when surveys were conducted in IO mode only. This method shows promise although further development is desirable to reduce the associated bias further, perhaps by including weather and school size as covariates.

## **INTRODUCTION**

Estimates of circumpolar abundance for Antarctic minke whales (*Balaenoptera bonaerensis*) have traditionally been obtained using the "standard" method of applying line transect methodology to the IDCR/SOWER sightings data (e.g. Branch and Butterworth, 2001). The standard method assumes that g(0) = 1, where g(y) is the probability of detecting a school at perpendicular distance y from the trackline, implying that no schools on the trackline are missed. Since some schools on the trackline undoubtedly are missed, estimates using the standard method will likely be negatively biased.

Three alternative methods (Cooke, 2001; Bravington, 2004; Okamura and Kitakado, 2004) attempt to address this problem by estimating g(0) from the Independent Observer (IO) data in the IDCR/SOWER surveys. In IO mode, sightings are recorded from two independent platforms. To test the efficacy of these new analytical methods, simulated IDCR/SOWER-like data were generated by Palka and Smith (2004; 2005). Analyses of these data using the standard method confirmed that the standard method produced negatively biased estimates of whale density (Branch 2005). There are several variants of line transect methodology that can be used to estimate whale density without assuming that g(0) = 1. In this paper we apply the "direct duplicate" method (Palka 1995) to the simulated data (Palka and Smith, 2004; 2005).

# **METHODS**

## Simulated survey data

Input data files were generated as described in Palka and Smith (2004; 2005). Each survey iteration was conducted for 30-120 days depending on the scenario. The survey vessel travelled perpendicular to the ice edge for 16 hours and then shifted 20 km to the east for the following day's survey. Half of the scenarios were conducted in independent observer (IO) mode, the other half alternated between IO mode and closing mode. Scenarios included various covariates or assumptions and were divided into the "2004" scenarios (sc01 to sc16) and the "2005" scenarios (sc17 to sc32). The simulations were never intended to mimic exactly the IDCR/SOWER survey conditions but instead to test estimation methods, therefore estimates of g(0) obtained from the simulated data are not indicative of the true g(0) encountered on the surveys. Some differences between the simulations and the IDCR/SOWER surveys were summarised in Branch (2005).

#### **Direct duplicate method**

The direct duplicate method uses standard distance sampling methodology to provide separate estimates of density from sightings made from the IO platform, the barrel (topman position), and those made from both platforms (duplicate sightings). The method then uses the Petersen two-sample mark-

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recapture equation to obtain the density of whales by treating the duplicates as "recaptures" of animals that were marked by one of the platforms. The overall estimated density of whales  $(D_w)$  is obtained from:

$$D_{w} = \frac{D_{w,lO} D_{w,topman}}{D_{w,duplicates}}$$
(1)

where:

 $D_{w IO}$  = density calculated from all sightings seen from the IO platform

 $D_{w,topman}$  = density calculated from all sightings seen from the topman position

 $D_{w,duplicates}$  = density calculated from all sightings that were seen by both the IO and topman positions.

Mark-recapture methods of estimating g(0) make the assumption of independence of sightings by different observers, so that bias is introduced when heterogeneity in sightability of observer efficiency results in violation of this assumption. The attractiveness of the direct duplicate method of g(0) estimation is that it requires the lesser assumption that independence applies only on the trackline, so that any bias resulting from non-independence is likely to be reduced (Buckland *et al.* 2004, p.133).

Two variants of this equation were needed, one for the scenarios that contained IO mode only data, and another for the scenarios consisting of alternating IO and closing mode data. For scenarios which consisted only of IO mode data, all sightings from the bridge were excluded and then the methods of Branch (2005) were applied to obtain the components of equation (1). Perpendicular distances had to be recalculated for duplicate and triplicate sightings because the perpendicular distance of the first such sighting had been recorded for all associated sightings in the simulated sightings files, but the direct duplicate method required platform-specific perpendicular distances.

For scenarios that consisted of a combination of IO and closing mode, the method above was used to obtain the estimated density of schools  $(D_s)$  from the IO mode portion of the surveys. The method could not be applied to the closing mode portion of the surveys since duplicate sightings were not recorded in closing mode. However, estimated school size,  $E[s]_{\text{closing}}$ , was obtained using closing mode sightings from all platforms, and then the estimated density of whales,  $D_w$ , was obtained as follows:

$$D_{s} = \frac{D_{s,\text{IO}}D_{s,\text{stopman}}}{D_{s,\text{duplicates}}}$$

$$D_{w} = D_{s} \cdot E[s]_{\text{closing}}$$
(2)

The conversion factor between IO and closing mode were not considered, nor did we calculate the inverse-variance weighted estimates of density obtained by combining IO mode estimates and closing mode estimates.

# RESULTS

#### **Results for "2004" scenarios**

Estimated effective search half width was much greater for the topman platform (mean across scenarios 1467 m, range 1112–1675 m, Table 1) than for the IO platform (mean 1149 m, range 823–1317 m), and was smallest for duplicate sightings (mean 895 m, range 569–1104 m). There was a strong correlation (across scenarios) between effective search half width recorded from the IO platform and the topman platform (r = 0.97), between the IO platform and duplicate sightings (r = 0.97) and between the topman and duplicate sightings (r = 0.91).

Estimated mean school size was generally close to the true values (Table 2). In scenarios with only IO mode, there was a tendency for mean school size to be greater when estimated effective search half

width was smaller, thus the largest mean school size estimates were obtained for duplicate sightings, and the smallest for topman sightings.

The estimated density of schools (and whales) was greatest when based on IO platform sightings, and least when based on duplicate sightings (Tables 3, 4).

There was a negative bias in whale density estimated by the direct duplicate method (mean -11%, range -31% to 8%, Table 4), but the estimates from individual iterations displayed a wide spread of values that generally spanned the true values (Figure 1). Estimated densities displayed greater negative bias when a density gradient was present (-14% vs. -8%), when the true detection function (i.e. that used to generate the simulated sightings) did not include school size as a covariate (-15% vs. -7%), and when the true detection function included weather as a covariate (-16% vs. -6%), but other factors had little influence on bias. The implied g(0) had a mean of 0.89 across scenarios (range 0.70 to 1.08).

### **Results for "2005" scenarios**

Similar patterns were obtained as for the "2004" scenarios: greatest effective search half width, smallest mean school size and highest density of schools was obtained from the topman platform, and the smallest search half width, largest mean school size and lowest density of schools was obtained from duplicate sightings, with estimates from the IO platform intermediate.

The estimated whale density from the direct duplicate method was negatively biased for 12 of 16 scenarios (mean bias -5%, range -19 to 10%, Table 4, Figure 2). Estimated density was more biased when school size errors were present (-7% vs. -4%), when density and weather were correlated (-12% vs. 1%), and when only IO mode survey was conducted (-11% vs. 0%), but the other factors had only a negligible impact on the bias associated with the estimated density of whales. The implied g(0) had a mean over scenarios of 0.95 (range 0.81 to 1.10).

# DISCUSSION

Estimated whale densities from the direct duplicate method were generally negatively biased (-11% for "2004" scenarios, -5% for "2005" scenarios) but less so than estimates from the standard method (-23% and -10% respectively (Branch 2005)). Compared to the standard method, similar factors caused negative bias: introducing school size and weather as covariates in the detection function, introducing errors in school size estimation, correlations between density and weather, and when surveys were conducted in IO mode only. It is interesting that estimates of density from simulated surveys in IO mode were negatively biased whereas simulations that also included closing mode were essentially unbiased. This effect likely resulted from negative bias in school size estimates during IO mode.

In summary, applying the direct duplicate method to IDCR/SOWER data would likely eliminate some of the negative bias from assuming that g(0) = 1, especially if closing mode estimates of school size were used. Further reduction in bias may be possible if covariates such as weather and school size were incorporated.

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|          | IO platform |       | Topman p | olatform | Duplicate sightings |       |  |
|----------|-------------|-------|----------|----------|---------------------|-------|--|
| Scenario | esw         | CV    | esw      | CV       | esw                 | CV    |  |
| sc01     | 1087        | 0.099 | 1377     | 0.086    | 899                 | 0.101 |  |
| sc02     | 1179        | 0.132 | 1487     | 0.073    | 909                 | 0.188 |  |
| sc03     | 1201        | 0.094 | 1543     | 0.074    | 912                 | 0.111 |  |
| sc04     | 1178        | 0.099 | 1536     | 0.081    | 893                 | 0.139 |  |
| sc05     | 1144        | 0.117 | 1459     | 0.079    | 849                 | 0.179 |  |
| sc06     | 1317        | 0.066 | 1675     | 0.068    | 1056                | 0.081 |  |
| sc07     | 823         | 0.101 | 1112     | 0.105    | 569                 | 0.175 |  |
| sc08     | 1317        | 0.131 | 1565     | 0.109    | 1104                | 0.162 |  |
| sc09     | 1127        | 0.109 | 1462     | 0.082    | 833                 | 0.153 |  |
| sc10     | 1246        | 0.086 | 1638     | 0.086    | 995                 | 0.106 |  |
| sc11     | 839         | 0.125 | 1120     | 0.088    | 591                 | 0.191 |  |
| sc12     | 1284        | 0.114 | 1554     | 0.096    | 1089                | 0.131 |  |
| sc13     | 1076        | 0.121 | 1373     | 0.093    | 875                 | 0.139 |  |
| sc14     | 1149        | 0.122 | 1462     | 0.088    | 899                 | 0.197 |  |
| sc15     | 1229        | 0.099 | 1579     | 0.078    | 959                 | 0.136 |  |
| sc16     | 1180        | 0.086 | 1524     | 0.067    | 886                 | 0.112 |  |
| sc17     | 910         | 0.113 | 1231     | 0.092    | 732                 | 0.150 |  |
| sc18     | 1293        | 0.100 | 1668     | 0.089    | 1042                | 0.117 |  |
| sc19     | 898         | 0.111 | 1215     | 0.087    | 718                 | 0.133 |  |
| sc20     | 1299        | 0.102 | 1661     | 0.090    | 1040                | 0.125 |  |
| sc21     | 1323        | 0.101 | 1675     | 0.083    | 1135                | 0.111 |  |
| sc22     | 916         | 0.106 | 1229     | 0.083    | 773                 | 0.125 |  |
| sc23     | 1308        | 0.100 | 1682     | 0.084    | 1105                | 0.121 |  |
| sc24     | 924         | 0.110 | 1254     | 0.091    | 775                 | 0.140 |  |
| sc25     | 1330        | 0.098 | 1674     | 0.102    | 1133                | 0.119 |  |
| sc26     | 929         | 0.115 | 1244     | 0.095    | 791                 | 0.147 |  |
| sc27     | 1324        | 0.120 | 1654     | 0.091    | 1110                | 0.130 |  |
| sc28     | 914         | 0.129 | 1228     | 0.096    | 774                 | 0.154 |  |
| sc29     | 897         | 0.101 | 1202     | 0.090    | 724                 | 0.125 |  |
| sc30     | 1295        | 0.103 | 1672     | 0.077    | 1035                | 0.109 |  |
| sc31     | 918         | 0.106 | 1240     | 0.093    | 737                 | 0.151 |  |
| sc32     | 1313        | 0.091 | 1665     | 0.073    | 1068                | 0.106 |  |

Table 1. Estimated effective search half-width (m) and associated CV for each scenario based on sightings in IO mode from the IO platform, from the topman platform and from duplicate sightings made from both the IO and topman platforms.

|          | IO platform Topman platform |       | Duplicate sightings |       | All platforms |       | -    |       |           |
|----------|-----------------------------|-------|---------------------|-------|---------------|-------|------|-------|-----------|
| Scenario | E[s]                        | CV    | E[s]                | CV    | E[s]          | CV    | E[s] | CV    | True E[s] |
| sc01     | _                           | -     | —                   | _     | _             | _     | 2.56 | 0.072 | 2.45      |
| sc02     | 2.35                        | 0.064 | 2.37                | 0.055 | 2.33          | 0.095 | _    | _     | 2.45      |
| sc03     | 2.04                        | 0.064 | 1.97                | 0.052 | 2.14          | 0.077 | _    | _     | 1.91      |
| sc04     | _                           | -     | _                   | _     | _             | _     | 2.09 | 0.059 | 2.04      |
| sc05     | _                           | _     | _                   | _     | _             | _     | 2.39 | 0.070 | 2.45      |
| sc06     | 2.58                        | 0.043 | 2.49                | 0.039 | 2.67          | 0.050 | _    | _     | 2.44      |
| sc07     | 1.87                        | 0.073 | 1.89                | 0.064 | 1.86          | 0.112 | _    | _     | 1.91      |
| sc08     | _                           | _     | _                   | _     | _             | _     | 2.21 | 0.078 | 2.04      |
| sc09     | 1.99                        | 0.072 | 1.97                | 0.051 | 1.99          | 0.085 | _    | _     | 2.02      |
| sc10     | _                           | _     | _                   | _     | _             | _     | 2.15 | 0.071 | 1.96      |
| sc11     | _                           | _     | _                   | _     | _             | _     | 2.37 | 0.054 | 2.44      |
| sc12     | 2.57                        | 0.069 | 2.53                | 0.063 | 2.66          | 0.082 | _    | _     | 2.44      |
| sc13     | 2.12                        | 0.065 | 2.05                | 0.059 | 2.19          | 0.084 | _    | _     | 2.03      |
| sc14     | _                           | _     | _                   | _     | _             | _     | 2.02 | 0.075 | 1.95      |
| sc15     | _                           | _     | _                   | _     | _             | _     | 2.54 | 0.049 | 2.45      |
| sc16     | 2.41                        | 0.056 | 2.41                | 0.046 | 2.41          | 0.073 | _    | -     | 2.45      |
| sc17     | 2.64                        | 0.068 | 2.58                | 0.054 | 2.76          | 0.086 | _    | _     | 2.45      |
| sc18     | 2.49                        | 0.061 | 2.38                | 0.063 | 2.61          | 0.068 | _    | _     | 2.45      |
| sc19     | _                           | _     | _                   | _     | _             | _     | 2.55 | 0.056 | 1.91      |
| sc20     | _                           | _     | _                   | _     | _             | _     | 2.55 | 0.083 | 2.04      |
| sc21     | 2.90                        | 0.056 | 2.72                | 0.057 | 3.29          | 0.063 | _    | _     | 2.45      |
| sc22     | 3.26                        | 0.068 | 3.08                | 0.053 | 3.79          | 0.087 | _    | _     | 2.44      |
| sc23     | _                           | _     | _                   | _     | _             | _     | 2.87 | 0.069 | 1.91      |
| sc24     | _                           | _     | _                   | _     | _             | _     | 3.06 | 0.055 | 2.04      |
| sc25     | _                           | _     | _                   | _     | _             | _     | 2.83 | 0.079 | 2.02      |
| sc26     | _                           | _     | _                   | _     | _             | _     | 3.05 | 0.067 | 1.96      |
| sc27     | 3.07                        | 0.063 | 2.88                | 0.059 | 3.41          | 0.079 | _    | _     | 2.44      |
| sc28     | 3.19                        | 0.061 | 2.99                | 0.051 | 3.76          | 0.075 | _    | _     | 2.44      |
| sc29     | _                           | _     | _                   | _     | _             | _     | 2.58 | 0.065 | 2.03      |
| sc30     | _                           | _     | _                   | _     | _             | _     | 2.50 | 0.083 | 1.95      |
| sc31     | 2.56                        | 0.058 | 2.47                | 0.048 | 2.67          | 0.070 | _    | _     | 2.45      |
| sc32     | 2.59                        | 0.060 | 2.51                | 0.058 | 2.68          | 0.074 | _    | _     | 2.45      |

Table 2. Estimated school size and associated CV for each of the scenarios. For scenarios which only contained IO mode data, estimated school size was calculated separately from sightings made from the IO platform, those made from the topman platform, and those made from both the IO and topman platforms. For scenarios which included closing mode data, the estimated school size was calculated from sightings made from all platforms during closing mode.

|          | IO platform |       | Topman p | olatform | Duplicate sightings |       |  |
|----------|-------------|-------|----------|----------|---------------------|-------|--|
| Scenario | Ds          | CV    | Ds       | CV       | Ds                  | CV    |  |
| sc01     | 0.0155      | 0.125 | 0.0191   | 0.099    | 0.0116              | 0.138 |  |
| sc02     | 0.0104      | 0.144 | 0.0132   | 0.083    | 0.0060              | 0.201 |  |
| sc03     | 0.0144      | 0.104 | 0.0190   | 0.077    | 0.0100              | 0.138 |  |
| sc04     | 0.0135      | 0.121 | 0.0165   | 0.089    | 0.0085              | 0.158 |  |
| sc05     | 0.0112      | 0.140 | 0.0162   | 0.100    | 0.0067              | 0.203 |  |
| sc06     | 0.0202      | 0.086 | 0.0235   | 0.078    | 0.0167              | 0.105 |  |
| sc07     | 0.0086      | 0.111 | 0.0107   | 0.113    | 0.0040              | 0.215 |  |
| sc08     | 0.0170      | 0.166 | 0.0194   | 0.137    | 0.0132              | 0.201 |  |
| sc09     | 0.0115      | 0.127 | 0.0161   | 0.086    | 0.0069              | 0.166 |  |
| sc10     | 0.0200      | 0.113 | 0.0232   | 0.088    | 0.0161              | 0.130 |  |
| sc11     | 0.0076      | 0.150 | 0.0094   | 0.099    | 0.0034              | 0.225 |  |
| sc12     | 0.0184      | 0.153 | 0.0205   | 0.127    | 0.0142              | 0.175 |  |
| sc13     | 0.0152      | 0.121 | 0.0187   | 0.098    | 0.0114              | 0.157 |  |
| sc14     | 0.0104      | 0.132 | 0.0132   | 0.100    | 0.0058              | 0.212 |  |
| sc15     | 0.0145      | 0.108 | 0.0188   | 0.081    | 0.0100              | 0.157 |  |
| sc16     | 0.0141      | 0.090 | 0.0176   | 0.075    | 0.0091              | 0.120 |  |
| sc17     | 0.0142      | 0.123 | 0.0174   | 0.099    | 0.0103              | 0.157 |  |
| sc18     | 0.0205      | 0.129 | 0.0238   | 0.091    | 0.0170              | 0.149 |  |
| sc19     | 0.0155      | 0.126 | 0.0188   | 0.092    | 0.0112              | 0.148 |  |
| sc20     | 0.0227      | 0.122 | 0.0266   | 0.101    | 0.0188              | 0.151 |  |
| sc21     | 0.0177      | 0.116 | 0.0208   | 0.093    | 0.0137              | 0.138 |  |
| sc22     | 0.0128      | 0.120 | 0.0157   | 0.095    | 0.0090              | 0.155 |  |
| sc23     | 0.0178      | 0.113 | 0.0208   | 0.090    | 0.0138              | 0.126 |  |
| sc24     | 0.0137      | 0.121 | 0.0164   | 0.107    | 0.0097              | 0.167 |  |
| sc25     | 0.0195      | 0.127 | 0.0233   | 0.110    | 0.0153              | 0.146 |  |
| sc26     | 0.0134      | 0.126 | 0.0163   | 0.108    | 0.0093              | 0.174 |  |
| sc27     | 0.0179      | 0.130 | 0.0212   | 0.101    | 0.0142              | 0.140 |  |
| sc28     | 0.0129      | 0.149 | 0.0156   | 0.113    | 0.0091              | 0.181 |  |
| sc29     | 0.0154      | 0.113 | 0.0191   | 0.092    | 0.0111              | 0.148 |  |
| sc30     | 0.0203      | 0.115 | 0.0237   | 0.095    | 0.0166              | 0.126 |  |
| sc31     | 0.0143      | 0.117 | 0.0174   | 0.103    | 0.0104              | 0.152 |  |
| sc32     | 0.0203      | 0.102 | 0.0238   | 0.076    | 0.0166              | 0.122 |  |

Table 3. Estimated density of schools based on IO platform sightings, topman platform sightings, and duplicate sightings from both the IO and topman platforms.

| Scenario | ΙΟ    | Topman | Duplicates | DD    | DD CV | True $D_w$ | Bias (%) | g(0) |
|----------|-------|--------|------------|-------|-------|------------|----------|------|
| sc01     | 0.040 | 0.049  | 0.030      | 0.066 | 0.144 | 0.072      | -8.3     | 0.92 |
| sc02     | 0.024 | 0.031  | 0.014      | 0.056 | 0.151 | 0.071      | -20.7    | 0.79 |
| sc03     | 0.029 | 0.038  | 0.021      | 0.052 | 0.098 | 0.056      | -6.7     | 0.93 |
| sc04     | 0.028 | 0.035  | 0.018      | 0.055 | 0.135 | 0.064      | -13.3    | 0.87 |
| sc05     | 0.027 | 0.039  | 0.016      | 0.066 | 0.157 | 0.071      | -7.7     | 0.92 |
| sc06     | 0.052 | 0.059  | 0.045      | 0.069 | 0.083 | 0.070      | -2.2     | 0.98 |
| sc07     | 0.016 | 0.020  | 0.007      | 0.045 | 0.187 | 0.055      | -19.3    | 0.81 |
| sc08     | 0.038 | 0.043  | 0.029      | 0.056 | 0.160 | 0.063      | -12.2    | 0.88 |
| sc09     | 0.023 | 0.032  | 0.014      | 0.054 | 0.149 | 0.058      | -7.7     | 0.92 |
| sc10     | 0.043 | 0.050  | 0.035      | 0.062 | 0.127 | 0.057      | 8.3      | 1.08 |
| sc11     | 0.018 | 0.022  | 0.008      | 0.051 | 0.177 | 0.073      | -30.5    | 0.69 |
| sc12     | 0.047 | 0.052  | 0.038      | 0.065 | 0.146 | 0.071      | -8.0     | 0.92 |
| sc13     | 0.032 | 0.038  | 0.025      | 0.050 | 0.110 | 0.058      | -14.8    | 0.85 |
| sc14     | 0.021 | 0.027  | 0.012      | 0.049 | 0.139 | 0.057      | -13.7    | 0.86 |
| sc15     | 0.037 | 0.048  | 0.025      | 0.070 | 0.114 | 0.077      | -9.8     | 0.90 |
| sc16     | 0.034 | 0.042  | 0.022      | 0.066 | 0.106 | 0.071      | -7.5     | 0.93 |
|          |       |        |            |       |       |            |          |      |
| sc17     | 0.037 | 0.045  | 0.028      | 0.060 | 0.127 | 0.071      | -15.4    | 0.85 |
| sc18     | 0.051 | 0.057  | 0.044      | 0.065 | 0.123 | 0.070      | -7.2     | 0.93 |
| sc19     | 0.040 | 0.048  | 0.029      | 0.066 | 0.124 | 0.074      | -10.6    | 0.89 |
| sc20     | 0.058 | 0.068  | 0.048      | 0.082 | 0.123 | 0.077      | 6.4      | 1.06 |
| sc21     | 0.051 | 0.057  | 0.045      | 0.065 | 0.113 | 0.072      | -9.8     | 0.90 |
| sc22     | 0.042 | 0.048  | 0.034      | 0.059 | 0.114 | 0.071      | -16.0    | 0.84 |
| sc23     | 0.051 | 0.060  | 0.040      | 0.077 | 0.143 | 0.071      | 8.3      | 1.08 |
| sc24     | 0.042 | 0.050  | 0.030      | 0.071 | 0.134 | 0.074      | -3.6     | 0.96 |
| sc25     | 0.055 | 0.066  | 0.043      | 0.085 | 0.136 | 0.077      | 10.0     | 1.10 |
| sc26     | 0.041 | 0.050  | 0.028      | 0.072 | 0.118 | 0.074      | -3.0     | 0.97 |
| sc27     | 0.055 | 0.061  | 0.048      | 0.069 | 0.106 | 0.071      | -1.9     | 0.98 |
| sc28     | 0.041 | 0.047  | 0.034      | 0.057 | 0.136 | 0.070      | -19.0    | 0.81 |
| sc29     | 0.040 | 0.049  | 0.029      | 0.069 | 0.129 | 0.074      | -6.3     | 0.94 |
| sc30     | 0.051 | 0.059  | 0.042      | 0.073 | 0.115 | 0.071      | 2.0      | 1.02 |
| sc31     | 0.037 | 0.043  | 0.028      | 0.057 | 0.141 | 0.071      | -18.9    | 0.81 |
| sc32     | 0.053 | 0.060  | 0.044      | 0.071 | 0.091 | 0.071      | -0.7     | 0.99 |

Table 4. Estimated density of whales obtained from the IO platform, the topman platform, duplicates, and using the direct duplicate (DD) method. The percent bias = 100(observed - actual)/actual and the implied g(0) are also shown.

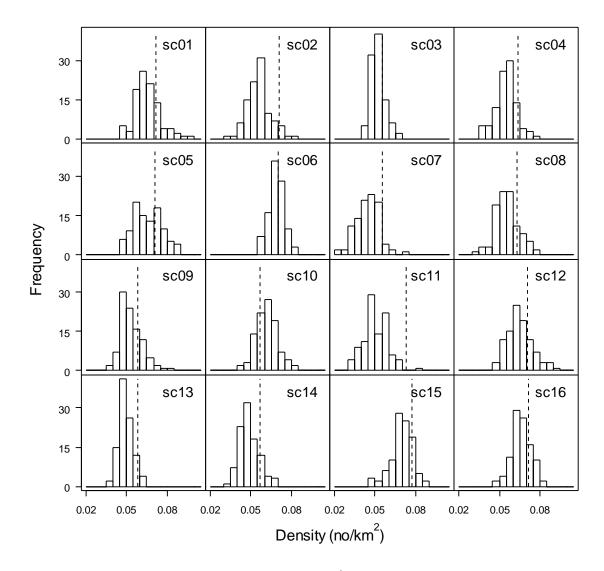


Figure 1. Histograms of estimated density (whales per  $km^2$ ) for each of the "2004" scenarios. The true mean values in the simulations are indicated by dashed vertical lines.

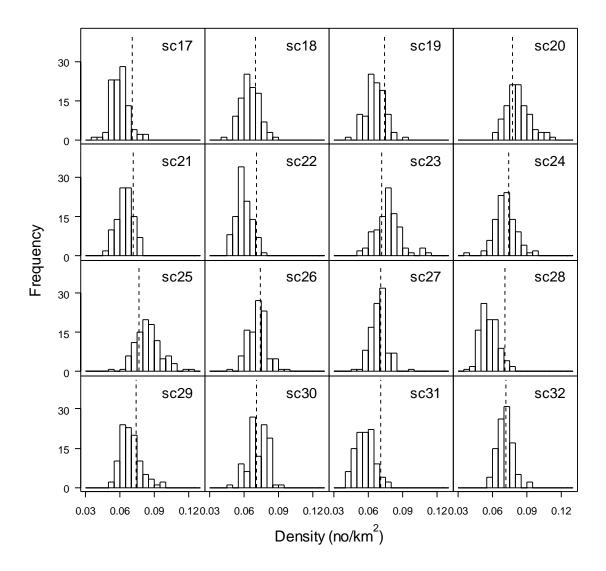


Figure 2. Histograms of estimated density (whales per  $km^2$ ) for the each of the "2005" scenarios. The true mean values in the simulations are indicated by dashed vertical lines.